

Vapor-Phase Mole Fractions Determined from the P, x Data Using the Margules Equation for High-Pressure Binary Vapor–Liquid Equilibrium Systems Including Carbon Dioxide

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ABSTRACT: High-pressure P, x data for CO₂ + hydrocarbons, methanol, ethanol, and water binaries were correlated using the Margules equation. The average relative difference between experimental data and the correlation was as low as 1 % at $T < T_{c1}$, where T and T_{c1} denote the system temperature and the critical temperature of the lighter component. It was found that the average relative difference of the vapor phase mole fractions from the Margules equation representing the P, x data is 0.6 % for the asymmetric and nonazeotropic binaries. A criterion for identifying the nonazeotropic binaries is proposed. The strength of molecular interactions and molecular order were identified for the azeotropic and zeotropic mixtures using partial molar excess enthalpies and entropies at infinite dilution. A method for the high-precision correlation of infinite dilution activity coefficients is proposed.

INTRODUCTION

High pressure binary vapor–liquid equilibria (VLE) for mixtures of carbon dioxide and light hydrocarbons are of practical importance for the optimum design of natural gas treatment processes.¹ Further, high-pressure VLE data for mixtures of CO₂ and alkanols, such as methanol and ethanol, are required for the process development of industrial immobilization for CO₂ byproducts.² In addition, VLE data for mixtures of CO₂ and water have become important for the rational design not only of industrial CO₂ immobilization² but also for biological carbon capture.³ Equations of state (EoS) combined with mixing rules have been known to satisfactorily correlate the high-pressure P, x data, as well as P, y data, for the mixtures including CO₂.^{4–9} However, investigations predicting thermodynamic properties including partial molar quantities at high pressures are rare. It was recently shown¹⁰ that high-pressure P, x data can be correlated simply using the Margules equation for few binaries including CO₂. Unfortunately, this promising method has not been applied to the calculation of P, y data and partial molar excess quantities that reflect the strength of molecular interactions and molecular order. Even for low-pressure VLE, the P, y data for azeotropic mixtures are not accurate.¹¹ Therefore, it is important for the practical treatment of high-pressure VLE data to determine if, for high-pressure nonazeotropic binaries, the P, y relationships are accurately calculated using the Margules equation derived from the P, x data. In addition, an advantage of the method using the Margules equation allows us to analyze the strength of the molecular interactions and molecular order even at high pressures.

The purpose of the present investigation is to show the following: (i) all of the high-pressure P, x data can be satisfactorily correlated using the Margules equation for the CO₂ + light hydrocarbons, methanol, ethanol, and water binaries; (ii) the Margules equation satisfactorily derives the P, y relationships of the nonazeotropic binaries identified by a criterion proposed in

the present investigation; and (iii) the strength of molecular interactions and molecular order for the azeotropic and zeotropic mixtures are identified using the partial molar excess enthalpies and entropies. To eliminate the obscurity arising from the definition of hypothetical liquids,^{10,12} constant temperature VLE data satisfying $T < T_{c1}$ are used, where T and T_{c1} denote the system temperature and the critical temperature of the lighter component. The present investigation proposes a practical calculation method for P, y relationships, because, in general, they involve higher experimental uncertainties than the P, x data.⁴

MODELS

Lumped Nonideality (LNI) Correlation. Binary vapor–liquid equilibria at constant temperature, T , are formulated as follows:¹³

$$Py_i = \Phi_i x_i P_{is} \quad (i = 1, 2) \quad (1)$$

$$\Phi_i = \gamma_i^{(P_s)} \frac{\phi_{is}}{\phi_i^V} \exp \frac{\bar{V}_i^L (P - P_a)}{RT} \exp \frac{V_i^o (P - P_{is})}{RT} \quad (2)$$

where x_i and y_i respectively denote the mole fractions of component i in the liquid phase and in the vapor phase. Equation 1 relates y_i to x_i . In eq 1, P and P_{is} are the system pressure and the vapor pressure of pure component i , respectively, while ϕ_i^V denotes the vapor phase fugacity coefficient of component i in the mixture at P and ϕ_{is} is the fugacity coefficient of the saturated vapor i at P_{is} . Furthermore, \bar{V}_i^L , V_i^o , and $\gamma_i^{(P_s)}$ respectively denote the partial molar volume of component i , the molar volume of

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Table 1. VLE Parameters and Data Sources for the CO₂ + Hydrocarbons, Water, Methanol, and Ethanol Binaries

system	T/K	T/T _{c1}	P _{1s} /MPa	P _{2s} /MPa	n ^a	x _{1min} ^b	x _{1max} ^{b,c}	A	B	(ARD) _p ^d	(ARD) _y ^e	χ ^f	Y ^g	ref
Symmetric and Azeotropic Mixtures														
CO ₂ (1) + ethane (2)	260.00	0.85	2.42	1.72	13	0	1	0.905	1.300	0.0071	0.1683	0.455	-0.685	15
CO ₂ (1) + ethane (2)	283.15	0.93	4.51	3.03	14	0	0.80	0.327	1.323	0.0122		0.724	-1.576	16
CO ₂ (1) + ethane (2)	269.25	0.89	3.14	2.18	15	0	1	0.674	1.283	0.0040		0.557	-0.906	16
CO ₂ (1) + ethane (2)	255.34	0.84	2.11	1.52	17	0	1	0.906	1.328	0.0053		0.408	-0.616	16
CO ₂ (1) + ethane (2)	241.45	0.79	1.35	1.01	11	0	1	0.984	1.447	0.0037		0.282	-0.465	16
CO ₂ (1) + ethane (2)	252.95	0.83	1.96	1.42	15	0	1	0.964	1.319	0.0032	0.0860	0.384	-0.561	17
CO ₂ (1) + ethane (2)	288.71	0.95	5.17	3.43	7	0.22	0.85	0.298	1.351	0.0109	0.2089	0.795	-2.042	18
CO ₂ (1) + ethane (2)	266.48	0.88	2.91	2.03	12	0.07	0.92	0.703	1.297	0.0121	0.1979	0.525	-0.845	18
CO ₂ (1) + ethane (2)	244.26	0.80	1.49	1.10	9	0.17	0.91	0.946	1.489	0.0098	0.0816	0.305	-0.543	18
CO ₂ (1) + ethane (2)	222.04	0.73	0.65	0.53	12	0.13	0.88	1.206	1.782	0.0054	0.0451	0.150	-0.366	18
CO ₂ (1) + ethane (2)	293.15	0.96	5.74	3.78	10	0	1	0.436	1.148	0.0074	0.2310	0.853	-1.709	19
CO ₂ (1) + ethane (2)	283.15	0.93	4.51	3.03	15	0	1	0.531	1.219	0.0069	0.1403	0.724	-1.318	19
CO ₂ (1) + ethane (2)	263.15	0.87	2.65	1.87	13	0	1	0.730	1.319	0.0040	0.0881	0.489	-0.784	19
CO ₂ (1) + ethane (2)	243.15	0.80	1.43	1.07	14	0	1	0.938	1.458	0.0048	0.0541	0.296	-0.500	19
CO ₂ (1) + ethane (2)	223.15	0.73	0.68	0.55	13	0	1	1.203	1.658	0.0046	0.0368	0.156	-0.325	19
CO ₂ (1) + ethane (2)	250.00	0.82	1.79	1.31	15	0	1	0.856	1.435	0.0044	0.0815	0.356	-0.608	19
CO ₂ (1) + ethane (2)	298.15	0.98	6.45	4.20	8	0	1	0.447	1.045	0.0037	0.3189	0.919	-1.726	20
CO ₂ (1) + ethane (2)	293.15	0.96	5.74	3.78	13	0	1	0.511	1.14	0.0077	0.2652	0.853	-1.682	20
CO ₂ (1) + ethane (2)	291.15	0.96	5.48	3.62	18	0	1	0.508	1.213	0.0089	0.1932	0.827	-1.777	20
CO ₂ (1) + ethane (2)	288.15	0.95	5.10	3.39	17	0	1	0.514	1.253	0.0042	0.1746	0.788	-1.692	20
CO ₂ (1) + ethane (2)	283.15	0.93	4.51	3.03	18	0	1	0.589	1.225	0.0022	0.1567	0.724	-1.332	20
CO ₂ (1)–ethylene (2)	263.15	0.93	2.65	3.24	13	0	1	0.495	0.531	0.0022	0.0443	0.555	-0.692	21
CO ₂ (1)–ethylene (2)	243.15	0.86	1.43	1.94	11	0	1	0.481	0.645	0.0066	0.0297	0.362	-0.417	21
CO ₂ (1)–ethylene (2)	223.15	0.79	0.68	1.07	13	0	1	0.572	0.709	0.0040	0.0278	0.207	-0.234	21
CO ₂ (1)–ethylene (2)	252.95	0.90	1.96	2.52	15	0	1	0.526	0.583	0.0027	0.0453	0.453	-0.524	21
CO ₂ (1)–ethylene (2)	231.55	0.82	0.95	1.39	12	0	1	0.555	0.758	0.0031	0.0296	0.266	-0.336	21
Av.										0.0058	0.1230			
Zeotropic Mixtures														
CO ₂ (1) + propane (2)	300.00	0.99	6.72	1.000	4	0.07	0.47	0.254	0.309	0.0078	0.2139	0.922	0.840	22
CO ₂ (1) + propane (2)	303.15	1.00	7.22	1.081	16	0	1	0.183	0.222	0.0064	0.1726	0.981	0.932	6
CO ₂ (1) + propane (2)	293.15	0.96	5.74	0.838	17	0	1	0.303	0.461	0.0043	0.1405	0.800	0.674	6
CO ₂ (1) + propane (2)	283.15	0.93	4.51	0.638	16	0	1	0.437	0.633	0.0042	0.1170	0.642	0.491	6
CO ₂ (1) + propane (2)	273.15	0.90	3.49	0.476	17	0	1	0.505	0.828	0.0052	0.0868	0.505	0.348	6
CO ₂ (1) + propane (2)	263.15	0.87	2.65	0.346	16	0	1	0.635	1.008	0.0071	0.0702	0.388	0.242	6
CO ₂ (1) + propane (2)	253.15	0.83	1.97	0.245	16	0	1	0.747	1.171	0.0070	0.0526	0.291	0.166	6
CO ₂ (1) + propane (2)	273.15	0.90	3.49	0.476	12	0	1	0.787	1.002	0.0141	0.0895	0.505	0.318	21
CO ₂ (1) + propane (2)	252.95	0.83	1.96	0.243	12	0	1	0.612	1.085	0.0163	0.0313	0.289	0.174	21
CO ₂ (1) + propane (2)	266.48	0.88	2.91	0.386	11	0.09	0.82	0.524	0.973	0.0215	0.0624	0.425	0.271	23
CO ₂ (1) + propane (2)	244.26	0.80	1.49	0.176	10	0.11	0.81	0.790	1.295	0.0094	0.0337	0.220	0.117	23
CO ₂ (1) + propane (2)	294.26	0.97	5.89	0.863	17	0	1	0.310	0.398	0.0032	0.1135	0.819	0.707	24
CO ₂ (1) + propane (2)	277.59	0.91	3.92	0.544	12	0	1	0.489	0.654	0.0062	0.0740	0.563	0.420	24
Av.										0.0087	0.0970			
Asymmetric and Nonazeotropic Binaries														
CO ₂ (1)–hexane (2)	298.15	0.98	6.45	0.020	10	0.05	0.89	0.318	0.204	0.0305	0.0122	0.874	0.872	25
CO ₂ (1)–benzene (2)	298.15	0.98	6.45	0.013	7	0.20	0.91	0.311	0.425	0.0216	0.0054	0.874	0.872	25
CO ₂ (1)–pentane (2)	277.65	0.91	3.93	0.030	12	0	1	0.575	0.634	0.0152	0.0093	0.534	0.526	26
CO ₂ (1)–methanol (2)	303.15	1.00	7.22	0.022	7	0.08	0.47	0.796	1.775	0.0104	0.0078	0.979	0.964	27
CO ₂ (1)–methanol (2)	298.15	0.98	6.45	0.017	6	0.10	0.54	0.642	1.894	0.0207	0.0077	0.874	0.860	27
CO ₂ (1)–methanol (2)	298.15	0.98	6.45	0.017	31	0.03	1	0.784	1.900	0.0236	0.0040	0.874	0.860	28
CO ₂ (1)–methanol (2)	293.15	0.96	5.74	0.013	7	0.06	1	0.819	1.848	0.0150	0.0006	0.778	0.768	28
CO ₂ (1)–methanol (2)	290.00	0.95	5.33	0.011	9	0.06	0.97	0.764	1.935	0.0253	0.0023	0.722	0.713	29

Table 1. Continued

system	T/K	T/T _{c1}	P _{1s} /MPa	P _{2s} /MPa	n ^a	x _{1min} ^b	x _{1max} ^{b,c}	A	B	(ARD) _p ^d	(ARD) _y ^e	X ^f	Y ^g	ref
CO ₂ (1)–methanol (2)	303.18	1.00	7.23	0.022	16	0.07	0.88	0.522	1.663	0.0181	0.0080	0.979	0.966	30
CO ₂ (1)–methanol (2)	298.16	0.98	6.45	0.017	17	0.07	0.88	0.593	1.645	0.0199	0.0075	0.874	0.864	30
CO ₂ (1)–methanol (2)	291.15	0.96	5.48	0.012	12	0.06	0.88	0.542	1.026	0.0128	0.0063	0.742	0.739	30
CO ₂ (1)–methanol (2)	298.15	0.98	6.45	0.017	8	0.06	0.90	0.620	1.663	0.0269	0.0044	0.874	0.863	25
CO ₂ (1)–methanol (2)	298.15	0.98	6.45	0.017	9	0.10	0.88	0.671	2.189	0.0166	0.0040	0.874	0.855	31
CO ₂ (1)–methanol (2)	288.15	0.95	5.10	0.010	7	0.11	0.84	0.841	2.355	0.0355	0.0014	0.691	0.677	31
CO ₂ (1)–ethanol (2)	303.15	1.00	7.22	0.010	9	0.06	0.91	0.694	1.701	0.0173	0.0041	0.979	0.972	32
CO ₂ (1)–ethanol (2)	293.15	0.96	5.74	0.006	8	0.05	0.81	0.804	1.855	0.0257	0.0014	0.778	0.773	32
CO ₂ (1)–ethanol (2)	298.00	0.98	6.42	0.008	9	0.01	0.03	0.850	2.473	0.0176	0.0000	0.870	0.859	33
CO ₂ (1)–ethanol (2)	303.13	1.00	7.22	0.010	11	0.10	0.85	0.432	1.214	0.0292	0.0097	0.978	0.975	30
CO ₂ (1)–ethanol (2)	298.17	0.98	6.45	0.008	8	0.13	0.81	0.104	1.089	0.0254	0.0093	0.874	0.871	30
CO ₂ (1)–ethanol (2)	303.12	1.00	7.22	0.010	11	0.10	0.85	0.432	1.214	0.0292	0.0097	0.978	0.975	34
CO ₂ (1)–ethanol (2)	298.17	0.98	6.45	0.008	8	0.13	0.81	0.104	1.089	0.0254	0.0093	0.874	0.871	34
Av.										0.0220	0.0059			
CO ₂ (1)–water (2)	298.28	0.98	6.46	0.003	7	0.003	0.023	3.10	16.4	0.0259		0.876	−5680	33
CO ₂ (1)–water (2)	288.26	0.95	5.11	0.002	7	0.004	0.028	3.07	14.8	0.0255		0.692	−638.0	33
CO ₂ (1)–water (2)	278.22	0.91	3.98	0.001	6	0.006	0.020	3.00	11.8	0.0063		0.540	−14.8	35
CO ₂ (1)–water (2)	293.00	0.96	5.72	0.002	9	0.001	0.002	3.21	11.7	0.0113		0.775	−35.9	35
CO ₂ (1)–water (2)	288.00	0.95	5.08	0.002	14	0.001	0.004	3.15	15.9	0.0165		0.688	−1800	35
Av.										0.0171				

^a Number of the data points. ^b Minimum x_1 value. ^c Maximum x_1 value. ^d Optimized average relative deviation, $(1/n)\sum|(P_{i,\text{exp}} - P_{i,\text{cal}})/P_{i,\text{exp}}|$. ^e Deviation in y_1 , $(1/n)\sum|(y_{i,\text{exp}} - y_{i,\text{cal}})/y_{i,\text{exp}}|$, where $y_{i,\text{cal}}$ was calculated from the Margules equation. ^f $(P_{1s} + P_{2s})/(P_{c1} + P_{2s})$. ^g $(P_{1s} - P_{2s}e^B)/(P_{c1} - P_{2s})$.

pure liquid i at T , and the activity coefficient of the component i in the liquid phase at $P = P_a$, a reference pressure. Hereafter, the P_a value is fixed at 0 for simplicity, and $\gamma_i^{(P_a)}$ is abbreviated as γ_i . The standard state for the activity of component i is the pure liquid of i at T and P_a . The lumped nonideality (LNI) correlation uses the Margules equation for formulating Φ_1 and Φ_2 as follows:¹⁰

$$\ln \Phi_1 = x_2^2[A + 2(B - A)x_1] \quad (3)$$

$$\ln \Phi_2 = x_1^2[B + 2(A - B)x_2] \quad (4)$$

$$A = \ln \Phi_1^\infty \quad B = \ln \Phi_2^\infty \quad (5)$$

where A and B denote the binary parameters. In the LNI correlation, the DECHEMA Chemistry Data Series analyzed low-pressure VLE data using the LNI correlation.¹¹ Meanwhile, Kato¹⁰ applied the LNI correlation to the high-pressure P , x data including the N₂ + O₂, CO₂ + ethane, CO₂ + decane, and CO₂ + methanol binaries. In the latter section, all of the binaries including CO₂ are correlated using the following optimization for the average relative deviation, (ARD)_p

$$(\text{ARD})_p = \frac{1}{n} \sum_{i=1}^n \left| \frac{P_{i,\text{exp}} - P_{i,\text{cal}}}{P_{i,\text{exp}}} \right| \quad (6)$$

where n denotes the number of the data points involved in one data set. The ratio of the fugacity coefficients of pure saturated vapors 1 and 2, ϕ_{1s}/ϕ_{2s} , is close to unity for the symmetric CO₂ + ethane and CO₂ + ethylene binaries. Therefore, in the latter section, it is shown that the LNI correlation satisfactorily represents the high-pressure P , x data for these symmetric systems. Furthermore, it is shown that the average deviation from the LNI correlation using 216 binaries including asymmetric systems is merely 0.9 %. An important advantage of the LNI correlation is that P , x data can be simply

correlated using the constant parameters, A and B , which are independent of composition and pressure, although the expression of nonideality is complicated as shown in eq 2. In the latter section, a high-precision correlation of temperature effects on the A and B parameters is proposed.

A Criterion Identifying Asymmetric and Nonazeotropic Binaries. Fixing the lighter component as component 1, minimum azeotropic mixtures may be characterized as follows:

$$\left. \frac{dP}{dx_1} \right|_{x_1=1} < 0 \quad \text{at} \quad T < T_{c1} \quad (7)$$

Using the Margules equation, the left-hand side of eq 7 is identical with $P_{1s} - P_{2s}e^B$. Therefore, in the present investigation, the following nondimensional formula is tested for categorizing the nonazeotropic binaries:

$$\frac{P_{1s} - P_{2s}e^B}{P_{c1} - P_{2s}} = \frac{P_{1s} + P_{2s}}{P_{c1} + P_{2s}} \quad (8)$$

At $T \rightarrow 0$ and $P \rightarrow 0$, both $X = (P_{1s} + P_{2s})/(P_{c1} + P_{2s})$ and $Y = (P_{1s} - P_{2s}e^B)/(P_{c1} - P_{2s})$ approach zero. One of the advantages of using X and Y is that $X = Y$ ($= P_{1s}/P_{1c}$), eq 8, holds for the asymmetric binaries satisfying $P_{1s} \gg P_{2s}$. Furthermore, X is an index of proximity ratio to critical points, because $X < 0.1$ and $X > 0.1$, respectively, hold for the low- and high-pressure VLE data. Finally, $Y < 0$ holds for the azeotropic mixtures.

Partial Molar Excess Enthalpies and Entropies. Assuming $\phi_i^V = \phi_{is}$ and $\exp[(V_i^o(P - P_{is}))/RT] = 1$ for the symmetric systems, the activity coefficient in eq 2 is approximated at infinite dilution as follows:

$$\gamma_i^\infty = \frac{\Phi_i^\infty}{\exp(\bar{V}_i^{L,\infty} p_{js}/RT)} \quad (9)$$

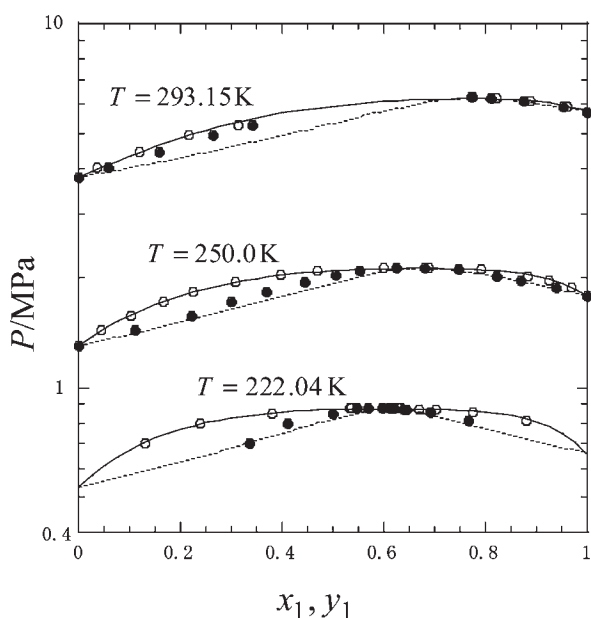


Figure 1. P vs x_1 and y_1 for the CO_2 (1) + ethane (2) binary at $T = 222.04$ K, 250.0 K, and 293.15 K: \circ , P , x data; \bullet , P , y data; —, P , x relationships correlated using the Margules equation; - - -, P , y relationships calculated by the Margules equation representing the P , x data; data were cited from Fredenslund and Mollerup¹⁸ at $T = 222.04$ K and Davalos et al. at $T = 250.0$ K and 293.15 K.¹⁹

where R denotes the gas constant. In the latter section, $\bar{V}_i^{L,\infty}$ was calculated using the nondimensional correlation proposed by Lyckman et al.¹⁴ The partial molar excess enthalpy and entropy at infinite dilution of the component i , $H_i^{E,\infty}$ and $S_i^{E,\infty}$, respectively, are defined as follows:

$$\ln \gamma_i^\infty = \frac{H_i^{E,\infty}}{RT_0} \frac{T_0}{T} - \frac{S_i^{E,\infty}}{R} \quad (10)$$

where $T_0 = 298.15$ K is used. In the latter section, assuming $\phi_i^V = \phi_{is}$ and $\exp[(V_i^o(P - P_{is}))/RT] = 1$ for the symmetric systems, the $H_i^{E,\infty}/RT_0$ and $S_i^{E,\infty}/R$ values are calculated from the $A = \ln \Phi_{1,\infty}$ and $B = \ln \Phi_{2,\infty}$ values representing the P , x data.

Data Sources. Table 1 lists the data sources^{15–35} used for the analysis. Six binaries, CO_2 (1) + ethane (2), CO_2 (1) + ethylene (2), CO_2 (1) + propane (2), CO_2 (1) + methanol (2), CO_2 (1) + ethanol (2), and CO_2 (1) + water (2), were extensively examined. The Wagner equation was used for calculating the vapor pressures of pure substances.⁴

RESULTS AND DISCUSSION

LNI Correlation. The Margules equation was fitted to the P , x data using the Marquardt method for determining the A and B parameters. The A and B values and the optimum $(\text{ARD})_P$ values are listed in Table 1. The average relative differences were 0.6 %, 0.4 %, and 0.9 % for CO_2 (1) + ethane (2), CO_2 (1) + ethylene (2), and CO_2 (1) + propane (2), respectively. The average $(\text{ARD})_P$ value of the six binaries is as low as 1.3 %, which is lower than the 1.8 % obtained from the 60 low-pressure VLE data sets of the methanol (1) + water (2) binary.¹¹ In Figure 1, P is plotted versus x_1 for the CO_2 (1) + ethane (2) binary at 222.04 K, 250.0 K, and 293.15 K. Figure 1 shows that the agreement between the experimental P , x data and their LNI correlations is excellent.

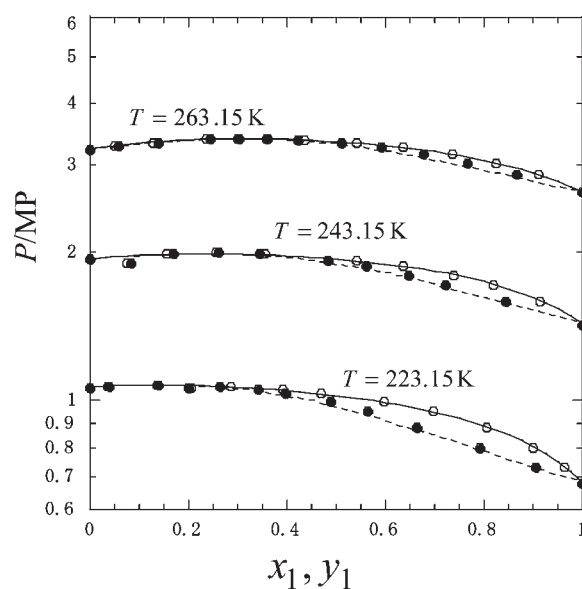


Figure 2. P vs x_1 and y_1 for the CO_2 (1) + ethylene (2) binary at $T = 223.15$ K, 243.15 K, and 263.15 K: \circ , P , x data; \bullet , P , y data; —, P , x relationships correlated using the Margules equation; - - -, P , y relationships calculated by the Margules equation representing the P , x data; data were cited from Nagahama et al.²¹

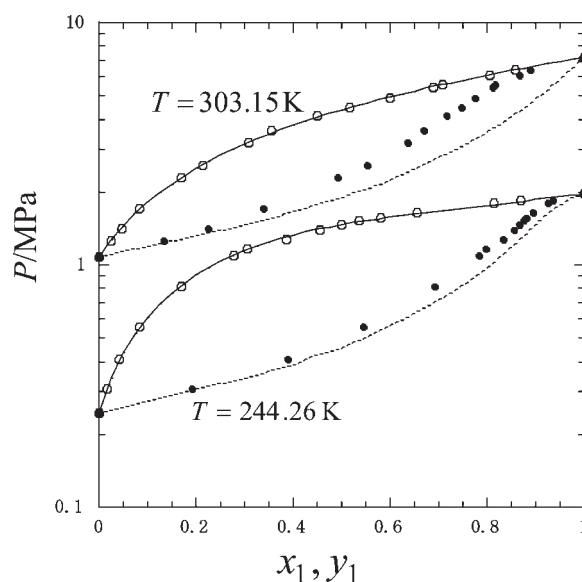


Figure 3. P vs x_1 and y_1 for the CO_2 (1) + propane (2) binary at $T = 244.26$ K and 303.15 K: \circ , P , x data; \bullet , P , y data; —, P , x relationships correlated using the Margules equation; - - -, P , y relationships calculated by the Margules equation representing the P , x data; data were cited from Hamam and Lu at $T = 244.26$ K²³ and Kim and Kim at $T = 303.15$ K.⁶

In Figures 2 to 5, P is plotted versus x_1 for the CO_2 (1) + ethylene (2), CO_2 (1) + propane (2), CO_2 (1) + pentane (2), and CO_2 (1) + methanol (2) binaries. Figures 1 to 5 show that the P , x data can be satisfactorily correlated by the Margules equation. Equations of state (EoS) also satisfactorily correlate the P , x data. If the P , x data for CO_2 (1) + propane (2) at 253.15 K $< T < 303.15$ K reported by Kim and Kim⁶ are used, the average relative differences from the Peng–Robinson equation of state (PR EoS) using interaction parameters involved in the mixing rules are as

Table 2. Correlation Deviations for the High- and Low-Pressure Binary P, x Data

	av.	asymmetric ^a	symmetric ^b	azeotropic
High-Pressure VLE Data ^{36,c}				
		(ARD) _P (no. data sets)		
Margules	0.009(216)	0.020(18)	0.0076(198)	0.0069(37)
Wilson	0.012(216)	0.032(18)	0.011(198)	0.010(37)
NRTL ^d	0.018(216)	0.059(18)	0.014(198)	0.016(37)
Low-Pressure VLE Data ¹¹				
		(ARD) _P from the Margules Equation (no. data sets)		
aqueous compounds	0.042(508)	-(0)	0.042(508)	0.048(268)
organic hydroxy compounds	0.027(1901)	0.024(64)	0.027(1837)	0.028(982)
aldehydes, ketones, ethers	0.012(1399)	0.010(92)	0.015(1307)	0.013(379)
carboxylic acids, anhydrides, esters	0.023(234)	0.016(5)	0.023(229)	0.031(57)
aliphatic hydrocarbons	0.012(1583)	0.018(108)	0.011(1475)	0.012(454)
aromatic hydrocarbons	0.010(1007)	0.024(60)	0.009(947)	0.007(108)
halogen, nitrogen, sulfur, and others	0.014(630)	0.016(59)	0.014(571)	0.015(134)

^a Asymmetric mixtures satisfy $p_{2s}/p_{1s} < 0.01$. ^b Symmetric mixtures satisfy $p_{2s}/p_{1s} > 0.01$. ^c Alkane + alkane binaries and binaries including CO₂ were eliminated. ^d Having a nonrandomness parameter of 0.3.

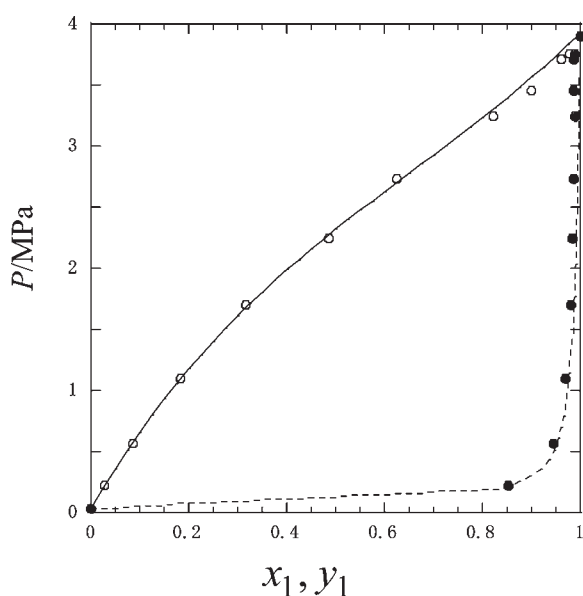


Figure 4. P vs x_1 and y_1 for the CO₂ (1) + pentane (2) binary at $T = 277.65$ K: ○, P, x data; ●, P, y data; —, P, x relationships correlated using the Margules equation; - - -, P, y relationships calculated by the Margules equation representing the P, x data; data were cited from Besserer and Robinson.²⁶

low as 1.1 %²² and 1.1 %.⁶ The same value, 1.1 %, was reported using perturbed chain polar statistical associating fluid theory (PCP-SAFT).⁸ Fortunately, the average (ARD)_P value for the same data at 253.15 K < T < 303.15 K is almost half, that is, 0.6 %, demonstrating that the LNI correlation using the Margules equation is simple but satisfactorily represents the P, x data albeit using two binary parameters rather than one interaction parameter. If the nonrandom two-liquid (NRTL) equation with a nonrandomness parameter of 0.3 and Wilson equations are used instead of the Margules equation, the average (ARD)_P values for the CO₂ (1) + propane (2) binary listed in Table 1 were 1 % and 0.9 %, respectively; that is, the Margules eq (0.9 %) provides an almost similar correlation.

As shown in Figures 1 to 3, the CO₂ (1) + ethane (2) and CO₂ (1) + ethylene (2) binaries form azeotropic mixtures, while the CO₂ (1) + propane (2) binary forms zeotropic mixtures. It is

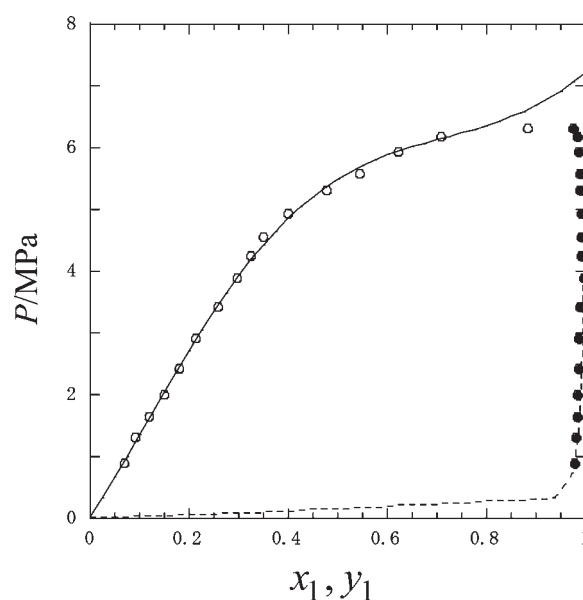


Figure 5. P vs x_1 and y_1 for the CO₂ (1) + methanol (2) binary at $T = 303.18$ K: ○, P, x data; ●, P, y data; —, P, x relationships correlated using the Margules equation; - - -, P, y relationships calculated by the Margules equation representing the P, x data; data were cited from Chang et al.³⁰

known that these symmetric systems show critical points at $T < T_{c1}$.⁵ However, as shown in Figure 5, even asymmetric and nonazeotropic binaries show the same trend; that is, critical points appear at $T < T_{c1}$. This occurs throughout the nonazeotropic binaries including CO₂ (1) + hexane (2), CO₂ (1) + benzene (2), CO₂ (1) + methanol (2), and CO₂ (1) + ethanol (2). This might be the main reason that the (ARD)_P values of the nonazeotropic binaries are higher than those of the azeotropic binaries. Similar results were obtained from the P, x data correlation using EoS and mixing rules.³⁶ As shown in Table 1, the average (ARD)_P value from the nonazeotropic binaries is still as low as 2.2 %. The value for the CO₂ (1) + water (2) binary is also as low as 1.7 % in spite of its narrow x_1 ranges covering $0 < x_1 < 0.03$.

In Table 2, the deviations from the LNI correlation for asymmetric and symmetric mixtures are listed for 216 high-pressure³⁶

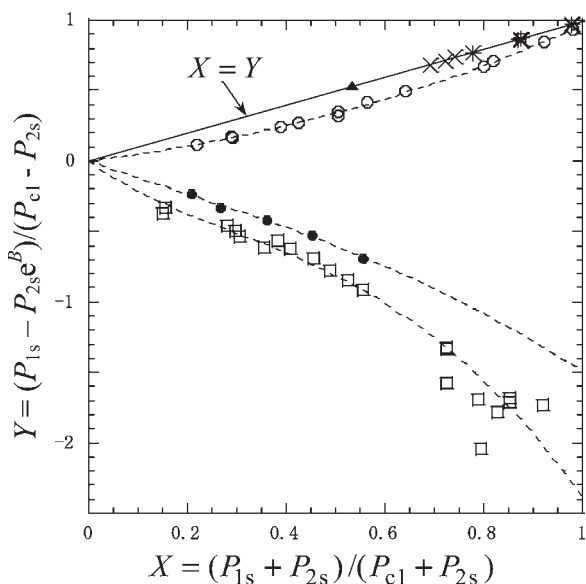


Figure 6. Y vs X : Δ , CO_2 (1) + hexane (2); ∇ , CO_2 (1) + benzene (2); \blacktriangle , CO_2 (1) + pentane (2); \times , CO_2 (1) + methanol (2); $+$, CO_2 (1) + ethanol (2); \circ , CO_2 (1) + propane (2); \bullet , CO_2 (1) + ethylene (2); \square , CO_2 (1) + ethane (2); $- -$, XY correlation.

and 7262 low-pressure¹¹ constant-temperature VLE data. Table 2 shows that the LNI correlation deviations from the Margules equation are notable for the low-pressure polar and symmetric binaries, which arises from azeotropic mixtures. Further, the correlation deviations of the high-pressure asymmetric binaries are as low as 2 % and almost identical with those of low-pressure asymmetric hydrocarbon binaries. Five of the 18 high-pressure asymmetric binaries satisfying $(\text{ARD})_p > 2$ % show notable data scatter, while the other four include alkanols, and they show the critical point deviations at $T < T_{c1}$. Therefore, these low quality high-pressure data may have caused the notable LNI correlation deviations. As shown in Table 2, the LNI characteristics of high-pressure binaries are similar to those of low-pressure nonpolar binaries; therefore, the Margules equation provides a better correlation than the Wilson and NRTL equations. In summary, Tables 1 and 2 show that the LNI correlation satisfactorily represents the P, x data of the high-pressure binaries covering $T < T_{c1}$.

y_1 Predicted from the P, x Data and the Criterion for Nonazeotropic Binaries. Using the Margules equation, average relative deviations from the P, y data were evaluated as follows:

$$(\text{ARD})_y = \frac{1}{n} \sum_{i=1}^n \left| \frac{y_{1i,\text{exp}} - y_{1i,\text{cal}}}{y_{1i,\text{exp}}} \right| \quad (11)$$

where $y_{1i,\text{cal}}$ was calculated by eqs 1, 3, and 4 with the A and B values representing the P, x data. Table 1 lists the $(\text{ARD})_y$ values. Figures 1 to 5 include the calculated P, y relationships as dashed lines. In low-pressure VLE, it is known that the P, y data of azeotropic binaries are less satisfactorily predicted from the P, x data. Figures 1 to 3 show that the agreement between experimental and predicted P, y relationships is worse at high pressures approaching the critical points. However, Figures 4 and 5 show that they are excellent for the nonazeotropic binaries. In reality, as shown in Table 1, the average $(\text{ARD})_y$ value of the nonazeotropic binaries approaches 0.6 %, which is much less than their average $(\text{ARD})_p$ value, 2.2 %. Therefore, to demonstrate the

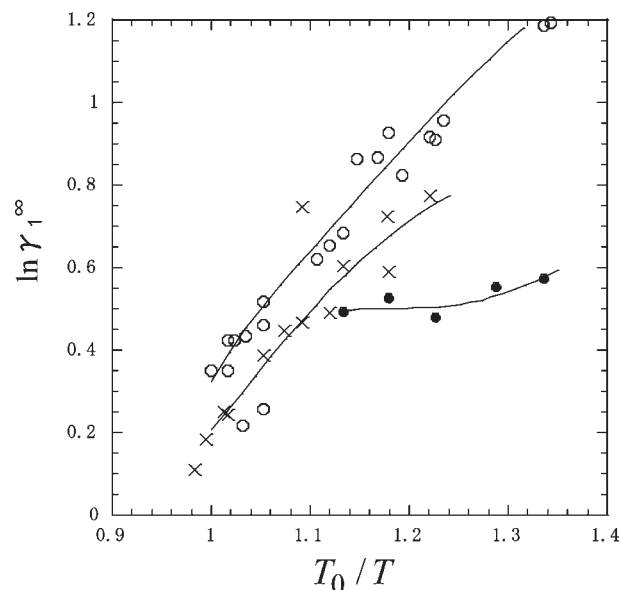


Figure 7. $\ln \gamma_1^\infty$ vs T_0/T : \circ , CO_2 (1) + ethane (2); \bullet , CO_2 (1) + ethylene (2); \times , CO_2 (1) + propane (2); $-$, predicted using the high-precision XZ correlation; $T_0 = 298.15$ K.

simple and practical method for the P, y relationships, the criterion for the nonazeotropic binary, eq 8, should be examined. In Figure 6, $Y = (P_{1s} - P_{2s}e^B)/(P_{c1} - P_{2s})$ is plotted versus $X = (P_{1s} + P_{2s})/(P_{c1} + P_{2s})$. Figure 6 clearly shows that all of the nonazeotropic binaries meet the criterion of $X = Y$. The zeotropic mixture, CO_2 + propane, slightly deviates from the $X = Y$ relationship, while the azeotropic mixture, CO_2 + ethane, is located at $Y < 0$. Therefore, for the high-pressure VLE at $T < T_{c1}$, the P, y relationship is accurately calculated from accurate P, x data using the Margules equation, if eq 8 is satisfied. The application of eq 8 to low-pressure azeotropic mixtures should be examined in the future.

Partial Molar Excess Enthalpies and Entropies. To determine the strength of molecular interactions and molecular order, in Figure 7, $\ln \gamma_1^\infty$ is plotted versus T_0/T for the CO_2 (1) + ethane (2), CO_2 (1) + ethylene (2), and CO_2 (1) + propane (2) binaries. The γ_1^∞ values were calculated from eq 9 using an empirical nondimensional correlation.¹³ Figure 7 shows that the scatter of infinite dilution activity coefficients is striking. Similar scatter appears in low-pressure data.¹¹ Without developing a high-precision correlation for the infinite dilution activity coefficients, it is impossible to determine accurate partial molar excess quantities. Fortunately, the data convergence of the data appearing in Figure 6 suggests a high-precision correlation of the infinite dilution activity coefficients. Therefore, the high-precision correlation for γ_2^∞ is obtained using the following X and Y , which reflects nondimensional infinite dilution pressure slope at $x_1 = 1$:

$$X = \frac{P_{1s} + P_{2s}}{P_{c1} + P_{2s}} \quad (12)$$

$$Y = \frac{P_{1s} - \gamma_2^\infty P_{2s}}{P_{c1} - P_{2s}} \quad (13)$$

The high-precision correlation for γ_1^∞ is obtained using X and the following Z , which reflects the nondimensional infinite

Table 3. High-Precision Correlation of Infinite Dilution Activity Coefficients

system	correlation ^a	(ARD) _Y ^b , (ARD) _Z ^c
CO ₂ (1)–ethane (2)	$Z = -13.2947X + 4.3611X^2 + 15.3639 \ln(1 + X)$ $Y = 21.083X - 7.0916X^2 - 23.6339 \ln(1 + X)$	0.11 0.07
CO ₂ (1)–ethylene (2)	$Z = -12.6176X + 5.2356X^2 + 12.8192 \ln(1 + X)$ $Y = 3.5324X - 1.7118X^2 - 4.787 \ln(1 + X)$	0.09 0.03
CO ₂ (1)–propane (2)	$Z = -6.3643X + 1.4943X^2 + 8.7428 \ln(1 + X)$ $Y = -0.4542X + 0.7864X^2 + 0.911 \ln(1 + X)$	0.05 0.02
CO ₂ (1)–water (2)	$Z = 24.5053X^{1.2697}$	0.05

^a $X = (P_{1s} + P_{2s}) / (P_{c1} + P_{2s})$. ^b $(ARD)_Y = (1/n) \sum |(Y_{i,exp} - Y_{i,cal}) / Y_{i,exp}|$. ^c $(ARD)_Z = (1/n) \sum |(Z_{i,exp} - Z_{i,cal}) / Z_{i,exp}|$.

Table 4. $H_i^{E,\infty}/RT_0$ and $S_i^{E,\infty}/R$ Values for CO₂ + Ethane, Propane, Ethylene, and Water Binaries at 280 K^a

system	$H_1^{E,\infty}/RT_0$	$S_1^{E,\infty}/R$	$H_2^{E,\infty}/RT_0$	$S_2^{E,\infty}/R$
CO ₂ (1) + ethane(2)	2.8 (2.7)	2.3 (2.2)	1.3	0.09
CO ₂ (1) + propane (2)	2.9 (2.6)	2.5 (2.2)	5.1	4.3
CO ₂ (1) + ethylene (2)	2.1 (0.84)	1.7 (0.63)	3.8	3.4
CO ₂ (1) + water (2)	-1.8 (-2.1)	-4.8 (-5.0)	-43	-59

^a $T_0 = 298.15$ K.

dilution pressure slope at $x_1 = 0$:

$$Z = \frac{\gamma_1^\infty P_{1s} - P_{2s}}{P_{c1} - P_{2s}} \quad (14)$$

In Table 3, the correlation functions of the high-precision correlation are listed for four binaries. Table 3 shows that the correlation deviations are satisfactorily low. In Figure 6, the Y values calculated using XY correlations are plotted using dashed lines. Figure 6 shows that the lines are identical with the converged XY data reported by different authors using different equipment; that is, these lines represent accurate VLE relationships. Therefore, the high-precision XY and XZ correlations are practically useful for calculating not only VLE relationships but also data consistency. Furthermore, they are expected to theoretically promote the development of solution models.

In Figure 7, $\ln \gamma_1^\infty$ is plotted using solid lines. Figure 7 shows that the XZ correlation represents the scattering of γ_1^∞ values. The partial molar excess quantities were calculated from eq 10 using the numerical differentiations of $\ln \gamma_i^\infty$ calculated from Y and Z in Table 3. In Table 4, the $H_i^{E,\infty}/RT_0$ and $S_i^{E,\infty}/R$ values at 280 K are listed. For convenience, hereafter, $H_{ij}^{E,\infty}$ denotes the partial molar excess enthalpy of component i at infinite dilution in component j . Table 4 demonstrates that the molecular interactions of hydrogen bonding in water are much stronger than the interactions in hydrocarbons, because $H_{CO_2,hydrocarbon}^{E,\infty} \gg H_{CO_2,water}^{E,\infty}$ holds, which reflects strong interactions between a CO₂ molecule and the surrounding water molecules. Note that the interaction strength of a CO₂ molecule with ethane and propane molecules is almost the same but is weaker than that with ethylene molecules, because $H_{CO_2,ethane}^{E,\infty} = H_{CO_2,propane}^{E,\infty} > H_{CO_2,ethylene}^{E,\infty}$ holds. Both molecular interactions and molecular order have effects on $\ln \gamma_i^\infty$, because the $H_i^{E,\infty}/RT_0$ and $S_i^{E,\infty}/R$ values are almost the same in magnitude. In Table 4, the values in parentheses were calculated assuming $\bar{V}_i^{L,\infty} = 0$. The values in parentheses provide almost the same insight obtained from $\bar{V}_i^{L,\infty} \neq 0$. Table 4 includes the $H_2^{E,\infty}/RT_0$ and $S_2^{E,\infty}/R$ values of infinitely diluted solutes in CO₂. In this case, the

standard states of activities are different in different solutes. However, Table 4 shows that propane in CO₂ exerts weak molecular interactions and molecular disorder, because the $H_{propane,CO_2}^{E,\infty}/RT_0$ and $S_{propane,CO_2}^{E,\infty}/R$ values are higher than those from ethane and ethylene. It is known that minimum azeotropic mixtures result from weak molecular interactions between solute and solvent molecules in the liquid phase.³⁷ Therefore, it might be that this weak molecular interaction originates the zeotropic behavior in spite of the nearly asymmetric CO₂ (1) + propane (2) binary. Table 4 includes the $H_{water,CO_2}^{E,\infty}/RT_0$ and $S_{water,CO_2}^{E,\infty}/R$ values, reflecting strong molecular interactions and high molecular order. Using infrared photodissociation spectra at 0.4 MPa, it has been identified that a water molecule is stabilized by the hydrogen bonding, OH–OCO, formed in the cluster involving seven CO₂ molecules;³⁸ therefore, the strong molecular interactions and high order may be ascribed to this hydrogen bonding in CO₂ clusters.

CONCLUSION

The correlation of high-pressure P , x data and the prediction of P , y relationships were investigated for the CO₂ + light hydrocarbons, methanol, ethanol, and water binaries, because they are important for the process development of natural gases, CO₂ immobilization, and biological carbon capture. It was shown that all of the P , x data can be satisfactorily correlated using the Margules equation. Furthermore, the Margules equation satisfactorily predicts the P , y relationships of the nonazeotropic binaries identified by the proposed criterion, eq 8. It was also shown that the slightly asymmetric and zeotropic CO₂ + propane binary has weaker molecular interactions and lower molecular order than the symmetric and azeotropic CO₂ + ethane binary. A method for the high-precision correlation of infinite dilution activity coefficients was proposed (readers can use the correlation at <http://www.sskato.jp>).

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